

# The Quadratic Formula

$$ax^2 + bx + c = 0$$

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The L<sup>A</sup>T<sub>E</sub>X Project

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- $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

# The Quadratic Formula

The solution of the quadratic equation.

$$ax^2 + bx + c = 0$$

where  $a$  is non-zero, is given by the formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$